# 6. Evolution, Co-evolution (and Artificial Life) Part 1

## Summary

- How can agents decide what to do (given some goals, knowledge and possible actions):
  - Rationality:
    - Individual utility maximisation (game theory, econ.)
    - Collective reasoning (Hobbs, Rawls, social contract)
  - Bounded rationality:
    - heuristics that attempt to achieve a goal (Schelling's segregation, Axelrod's tournament strategies)
  - Evolutionary / Adaptive
    - Individual learning (reinforcement, neural nets)
    - Social / evolutionary learning (genetic algorithms, genetic programming, co-evolutionary systems, cultural evolution)

#### What is evolution?

- It is a very old idea that predates modern science
- It is a theory of change
- Originally applied to human societies and ideas – because people could see these changed over time
- It isn't until recently (fossils etc) that it was realised biological life forms changed over time

# Biological evolution

- Evolution in everyday language has come to mean biological evolution
- Darwin did his famous empirical work observing biological organisms
- Biological evolution draws on empirical facts and theoretical models (often mathematical)
- Here we will focus on "abstract evolution" simulated in computer programs

#### Abstract evolution

- Evolution can be viewed as an algorithmic abstraction that can be used to understand / implement a process of change given:
  - Things that replicate / get copied (units of selection)
  - Variation in replicators (mutation)
  - Differential selection of replicators
- "fitness" means how good a replicator is at replicating (how many copies are made)
- In this context "survival of the fittest" is a tautology

Book: Daniel Dennett (1995) Darwin's Dangerous Idea. Simon & Schuster

# Abstract evolution (GA's)

- Genetic algorithms (which I think you know)
- Are an optimisation technique
- Define a space of solutions to a problem
- Code different candidate solutions in an "artificial chromosome" (often a bitstring but not always)
- Use an evolutionary algorithm to adapt solutions towards better (hopefully optimal or good enough) solutions
- Do this through some form of selection, recombination (crossover), mutation and reproduction
- John Holland early 70's, Alan Turing 50's, other earlier thinkers...

Book: Holland, John (1975). Adaptation in Natural and Artificial Systems.

Cambridge, MA: MIT Press

## Genetic Algorithms

- Initialise a population of (N) random chrom.
- Loop for some (G) number of generations
  - Loop for each chrom.
    - Test chrom. against an objective function f() award a fitness score
  - End loop solutions
  - Reproduce chrom probabilistically proportionally into the next generation based on fitness score
  - Apply some genetic operator (such as crossover)
  - Mutate reproduced chrom. with small prob. (m)
- End loop generations

# Reproduction / Selection

- Many ways to simulate reproduction:
  - Roulette Wheel Selection
  - Tournament Selection
  - Other kinds…
- In general you want an easy to implement and fast method
- That will allow for fitter solutions to tend to increase in the population over time

#### Roulette Wheel Selection

- Suppose you have a population of chromosomes and each has been allocated a fitness based on f()
- Add up the fitness's of all chromosomes = tf
- Repeat until next generation is full:
  - Generate a random number R in that range 0..tf
  - Select the first chromosome in the population that when all previous fitness's are added - gives you at least the value R
  - Reproduce the selected chrom. Into the next generation
- Hence it is like a roulette wheel where each spot on the wheel (representing a chromosome) is the size of the fitness of the associated chromosome

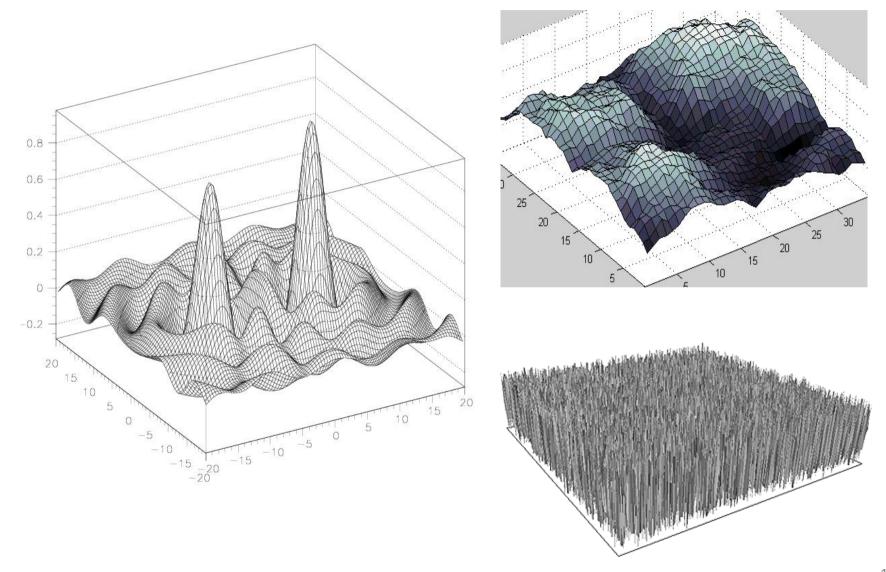
#### Tournament selection

- Many variants but a very simple form is:
- Repeat until next generation is full
  - Select pairs of chromosomes randomly
  - Reproduce the one with the highest fitness
  - Or a random one if they have same fitness

# Genetic Algorithms (crossover)

- You have to choose, G, N, m and f()
- Often GA's use crossover (recombination) of reproduced chromosomes as well as mutation
- This involves splicing together parts of chromosomes
- Can be compared to sexual reproduction
- 1-point crossover: take two chrom., select a random cut-point and spice together the chrom. of the two parents
- Holland developed "Schema Theory" to understand how various genetic operators (such as crossover) work
- Using GA's for optimisation very much an "art"
- There is no "free lunch" for search problems!

# Fitness landscapes



# Complex / implicit fitness function

- Can we still use evolutionary algorithms without simple explicit fitness functions?
- Yes, simple way, let a person look at solutions and select some they like better
- Dawkins "bimorphs" (NetLogo model library: biology/evolution/sunflower biomorphs)
- OR somehow let the "world" supply the fitness function – or a simulation of the world
- Evolving robots with "real physics"

#### Co-evolution fitness functions

- Suppose our solutions are "agents" that must interact socially with each other in a simulated environment to gain fitness
- The fitness of an agent depends on how the other agents behave
- Remember Axelrod's tournaments?
- To get a score (or fitness) for each algorithm he had to play them off in simulated tournaments
- Since the fitness of any agent is dependent on the other agents in the population
- This is called **co-evolution** because each agent evolves relative to the others rather than optimising an exogenous fixed fitness f()
- In this sense f() takes as inputs all the other agents
- When the agents are strategies in a simple game with known payoffs this relates to evolutionary game theory

# An evolutionary PD game

#### Suppose:

- agents as 1 bit strategy in the PD game where 1 = coop and 0 = defect
- population of N agents initialised at random (0 or 1)
- Apply an evolutionary algorithm where each generation each agent is randomly paired with some other agent in the population and plays a game of PD
- Reproduction (roulette wheel) using average payoff from the games as the fitness of each agent
- Apply some small (m = 0.01) mutation to each reproduced agent that causes it to flip its strategy

# **Evolving PD strategies**

- Initialise population N to random strategies
- Loop some number of generations
  - Loop for each agent (a) in the population
    - Select another agent (b) at random from the population
    - Play PD between (a) and (b) based on their strategies accumulate payoffs in agents
  - End loop for each agent
  - Reproduce a new population of size N probabilistically in proportion to average payoff and apply mutation with probability m
- End loop for number of generations

Note: Random pairing of strategies is sometimes called "mean field" interaction or "homogenous mixing". Reproduction without cross-over is called "asexual reproduction".

# **Evolving PD strategies**

- In this case with simple (pure) PD strategies and mean field mixing...
- Evolution will quickly lead to all defect dominating the population and stay there
- This is called an Evolutionary Stable Strategy (or ESS)
- A strategy is an ESS if a population all using it can resist "invasion" by a small number of any other strategy
- All ESS are Nash Equlibria (NE) but not all NE are ESS.
- Hence a link is found between game theory and evolutionary theory which biologists discovered and applied

Book: John Maynard Smith (1982) Evolution and the theory of games. Oxford University Press

# Sociobiology

- More generally the application of biological evolutionary approaches to understand social interactions is called Sociobiology
- When it is applied to human social systems it is can be highly controversial
- Critics worry it starts to look like "Social Darwinism" and overlooks the role of culture as the determinant of human social systems and behaviour
- We will not discuss this controversy here but it is worthwhile to be aware of it

Book: E. O. Wilson (1975) Sociobiology: The New Synthesis.

# **Evolving PD strategies**

- More complex strategies can be evolved in this way and analysed to see if they are ESS
- Axelrod noted in his book that tit-for-tat was "collectively stable" (almost an ESS)
- The relationship between ESS, Nash and, say,
  Pareto efficiency is subtle and complex even in mean field models
- However analysis (not just simulation) can be applied to simple games with a limited number of strategies

Paper: Nowak, Sigmund, Esam (1995) Automata, repeated games and noise. J.

Math. Biol. 33: 703-722

# **Evolution of strategies**

- Even if we can calculate some ESS for given a given system this does not necessarily tell us the dynamics (trajectories) that evolution will take from any given starting point
- In simple systems "replicator dynamics" equations can be used to prove things (assuming no mutation!)
- In general, simulation experiments are used to see what happens when it gets complicated

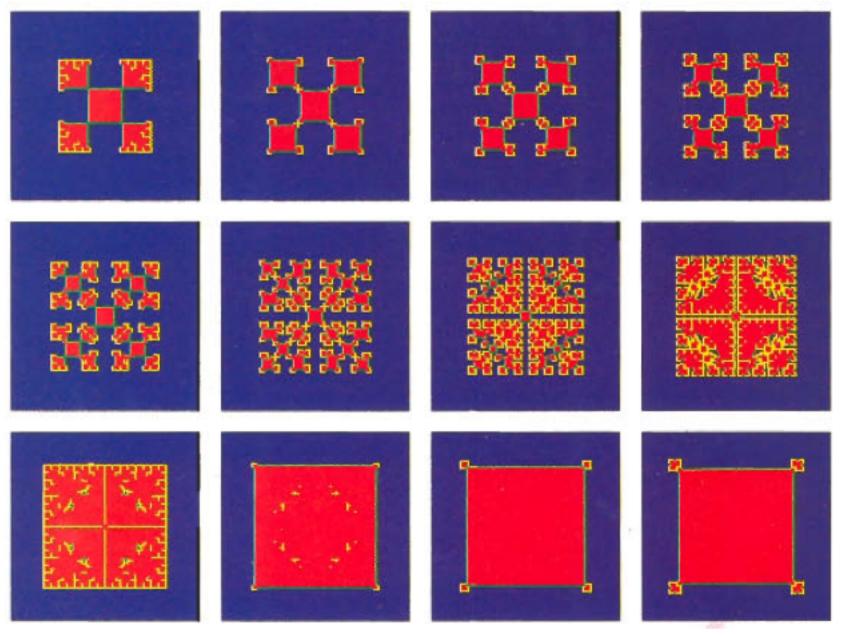
#### Non-random interactions

- Many forms of interaction in the "real world" are non-random
- Some work has explored this using a cellular automata (CA) where:
  - Each cell is either coop or defect state
  - Plays PD with each of it's neighbours (and possibly itself)
  - Copies the the strategy of fittest neighbour (or stays same if it is fittest)
  - Sometimes mutation is used sometimes not

# Evolving PD on a CA

- In general it has been found that over a broad range of parameters:
  - Cooperation can be sustained
  - Dynamic patterns emerge over time
  - Groups of cooperators and defectors because they are spatially clustered create these interesting dynamics
  - Pretty patterns can be produced
- The argument is that many biological and social phenomena interact in space and this can be a major factor in sustaining the evolution of cooperation

Paper: Nowak, May (1993) The Spatial Dilemmas of Evolution. Int. J. of Bifurcation and Chaos, Vol. 3, No. 1. 35-78



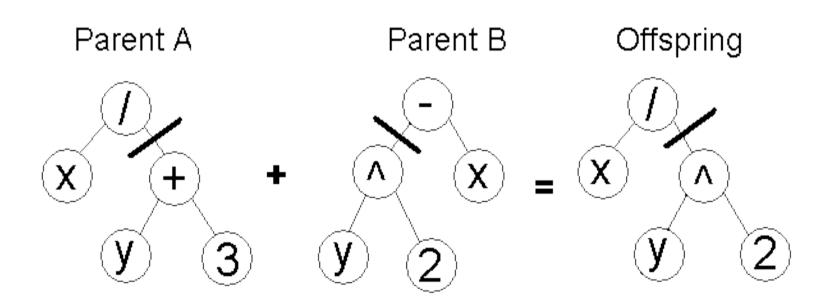
Taken from Nowak and May (1992)

# Unknown coding of solution?

- Suppose we don't have simple space of solutions (or strategies) that each "chromosome" can code
- Can we use evolutionary algorithms without a simple coding of the solution space?
- Yes, evolve a computer program directly (or an artificial neural network)
- Genetic Programming (GP) uses simple (functional) languages and tree-like crossovers
- Such languages have to be "robust" to mutation and crossover i.e. not "brittle" (unlike most computer languages where if you change one thing it breaks)
- In general GP are used to evolve small programs (or functions) for optimisation purposes

Book: Koza, J.R. (1992). Genetic Programming: On the Programming of Computers by Means of Natural Selection, MIT Press.

# **Genetic Programming**



It is possible to evolve whole programs like this but only small ones. Large programs with complex functions present big problems

# Readings and Questions

#### Readings

- Flake (1998) Chapter 5 Adaptation
- Gilbert et al (2005) Chapter 10 Learning and Evo. models

#### Questions

- Some claim TFT in the PD is an ESS others say it's not strictly an ESS. Can you think of a simple strategy that could invade a population all paying TFT?
- What would happen if we allowed agents to move on the grid based, in some way, on game payoff?
- "All evolution is co-evolution!" Is this true?
- Why do you think GP struggles to evolve large programs?