

Introduction to Genetic Algorithms

Guest speaker:

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Genetic Algorithms - History

- Pioneered by John Holland in the 1970's
- Got popular in the late 1980's
- Based on ideas from Darwinian Evolution
- Can be used to solve a variety of problems that are not easy to solve using other techniques

Evolution in the real world

- Each cell of a living thing contains *chromosomes* - strings of *DNA*
- Each chromosome contains a set of *genes* - blocks of DNA
- Each gene determines some aspect of the organism (like eye colour)
- A collection of genes is sometimes called a *genotype*
- A collection of aspects (like eye colour) is sometimes called a *phenotype*
- Reproduction involves recombination of genes from parents and then small amounts of *mutation* (errors) in copying
- The *fitness* of an organism is how much it can reproduce before it dies
- Evolution based on “survival of the fittest”

Start with a Dream...

- Suppose you have a problem
- You don't know how to solve it
- What can you do?
- Can you use a computer to somehow find a solution for you?
- This would be nice! Can it be done?

A dumb solution

A “blind generate and test” algorithm:

Repeat

 Generate a random possible solution

 Test the solution and see how good it is

Until solution is good enough

Can we use this dumb idea?

- Sometimes - yes:
 - if there are only a few possible solutions
 - and you have enough time
 - then such a method *could* be used
- For most problems - no:
 - many possible solutions
 - with no time to try them all
 - so this method *can not* be used

A “less-dumb” idea (GA)

Generate a *set* of random solutions

Repeat

- Test each solution in the set (rank them)

- Remove some bad solutions from set

- Duplicate some good solutions

 - make small changes to some of them

Until best solution is good enough

How do you encode a solution?

- Obviously this depends on the problem!
- GA's *often* encode solutions as fixed length “bitstrings” (e.g. 101110, 111111, 000101)
- Each bit represents some aspect of the proposed solution to the problem
- For GA's to work, we need to be able to “test” any string and get a “score” indicating how “good” that solution is

Silly Example - Drilling for Oil

- Imagine you had to drill for oil somewhere along a single 1km desert road
- Problem: choose the best place on the road that produces the most oil per day
- We could represent each solution as a position on the road
- Say, a whole number between [0..1000]

Where to drill for oil?

Solution1 = 300

Solution2 = 900



Road

0

500

1000

Digging for Oil

- The set of all possible solutions $[0..1000]$ is called the *search space* or *state space*
- In this case it's just one number but it could be many numbers or symbols
- Often GA's code numbers in binary producing a bitstring representing a solution
- In our example we choose 10 bits which is enough to represent $0..1000$

Convert to binary string

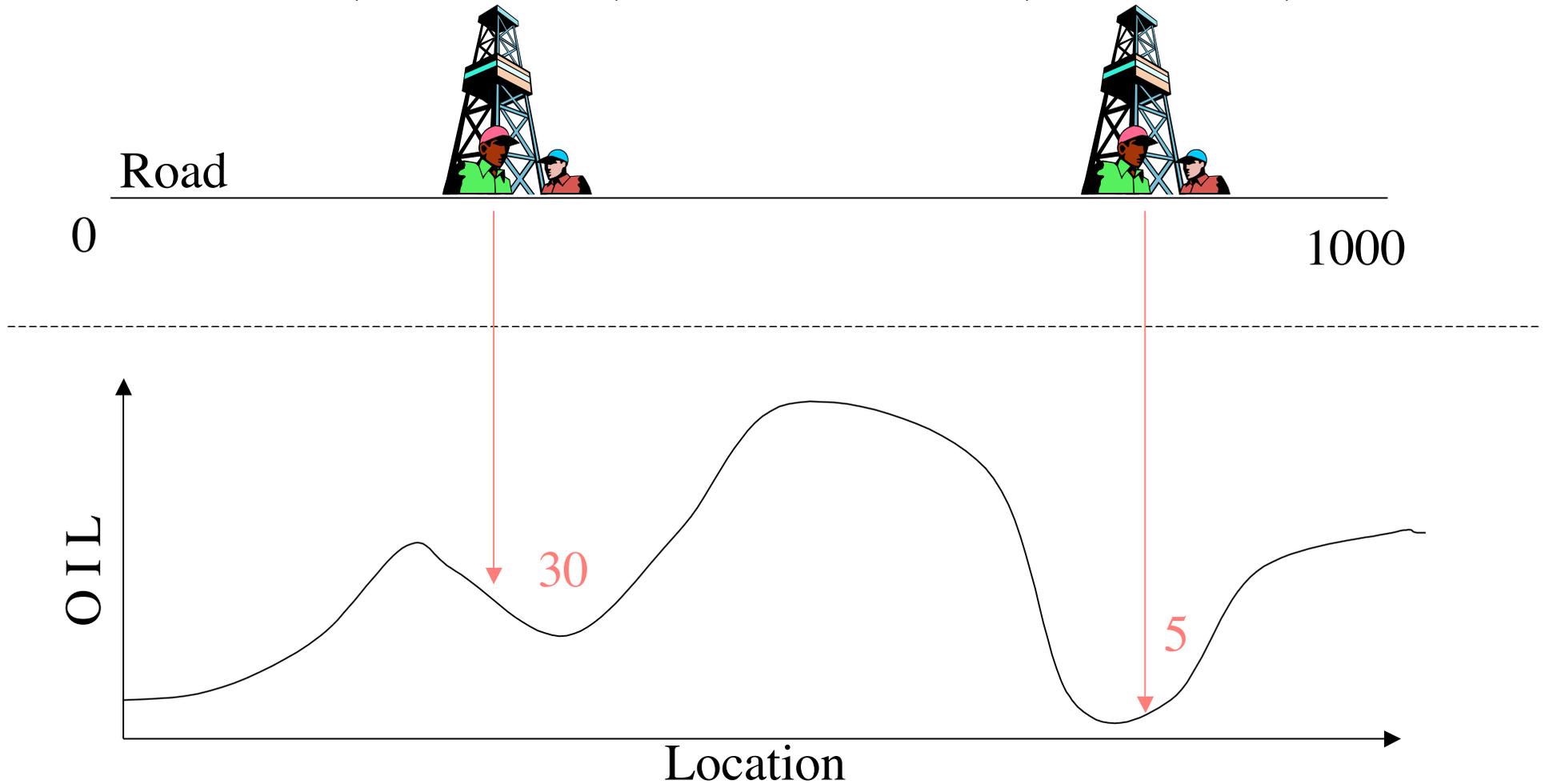
| | 512 | 256 | 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 |
|------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 900 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 300 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 |
| 1023 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

In GA's these encoded strings are sometimes called "*genotypes*" or "*chromosomes*" and the individual bits are sometimes called "*genes*"

Drilling for Oil

Solution1 = 300
(0100101100)

Solution2 = 900
(1110000100)



Summary

We have seen how to:

- represent possible solutions as a number
- encoded a number into a binary string
- generate a score for each number given a *function* of “how good” each solution is - this is often called a *fitness function*

Back to the (GA) Algorithm

Generate a *set* of random solutions

Repeat

- Test each solution in the set (rank them)

- Remove some bad solutions from set

- Duplicate some good solutions

 - make small changes to some of them

Until best solution is good enough

Replication and Mutation

- Various methods inspired by Darwinian evolution are used to update the set or *population* of solutions (or *chromosomes*)
- Two high scoring “parent” bit strings or *chromosomes* are selected and combined
- Producing two new *offspring* (bit strings)
- Each offspring may then be changed randomly (*mutation*)

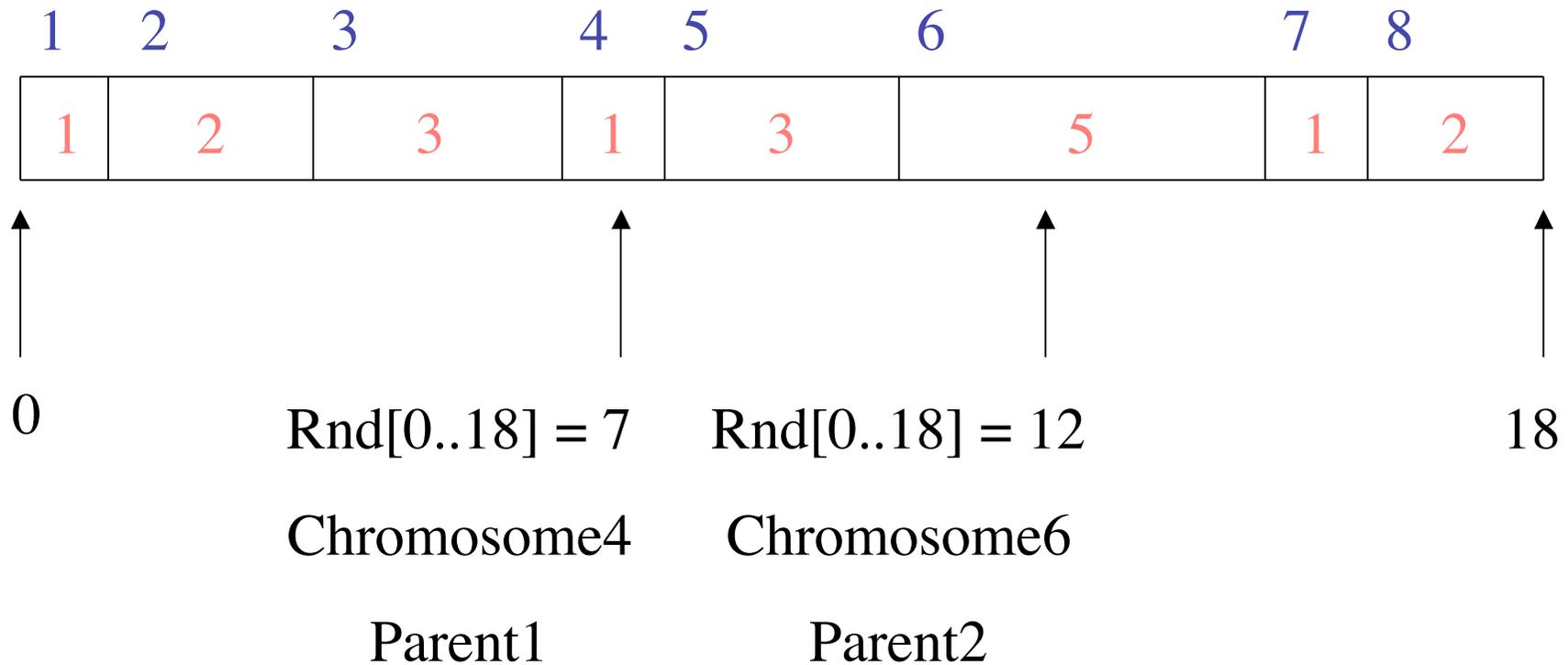
Selecting Parents

- Many schemes are possible so long as better scoring chromosomes more likely selected
- Score is often termed the *fitness*
- “Roulette Wheel” selection can be used:
 - Add up the fitness's of all chromosomes
 - Generate a random number R in that range
 - Select the first chromosome in the population that - when all previous fitness's are added - gives you at least the value R

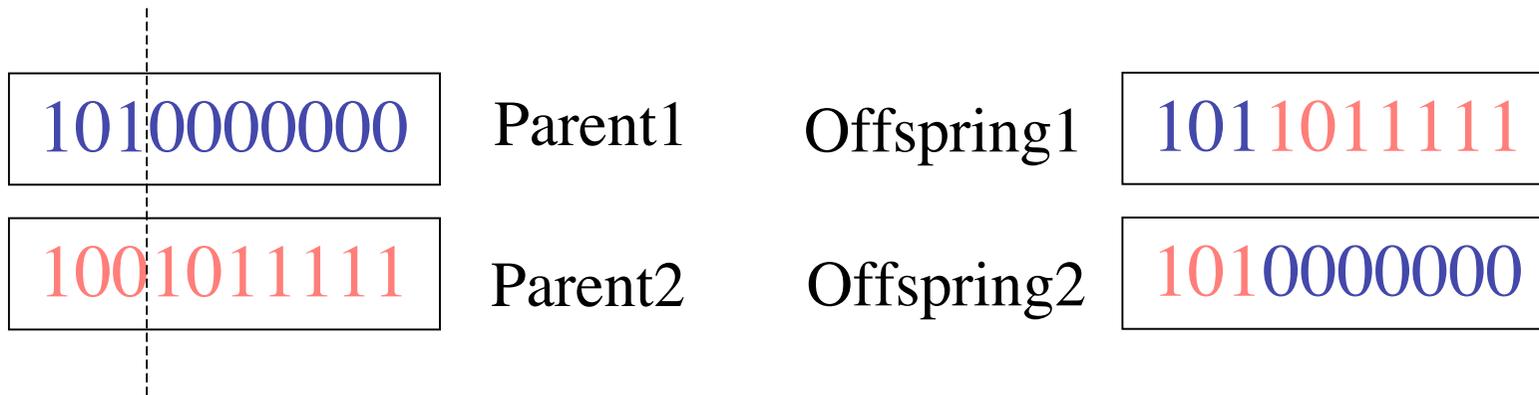
Example population

| No. | Chromosome | Fitness |
|-----|------------|---------|
| 1 | 1010011010 | 1 |
| 2 | 1111100001 | 2 |
| 3 | 1011001100 | 3 |
| 4 | 1010000000 | 1 |
| 5 | 0000010000 | 3 |
| 6 | 1001011111 | 5 |
| 7 | 0101010101 | 1 |
| 8 | 1011100111 | 2 |

Roulette Wheel Selection

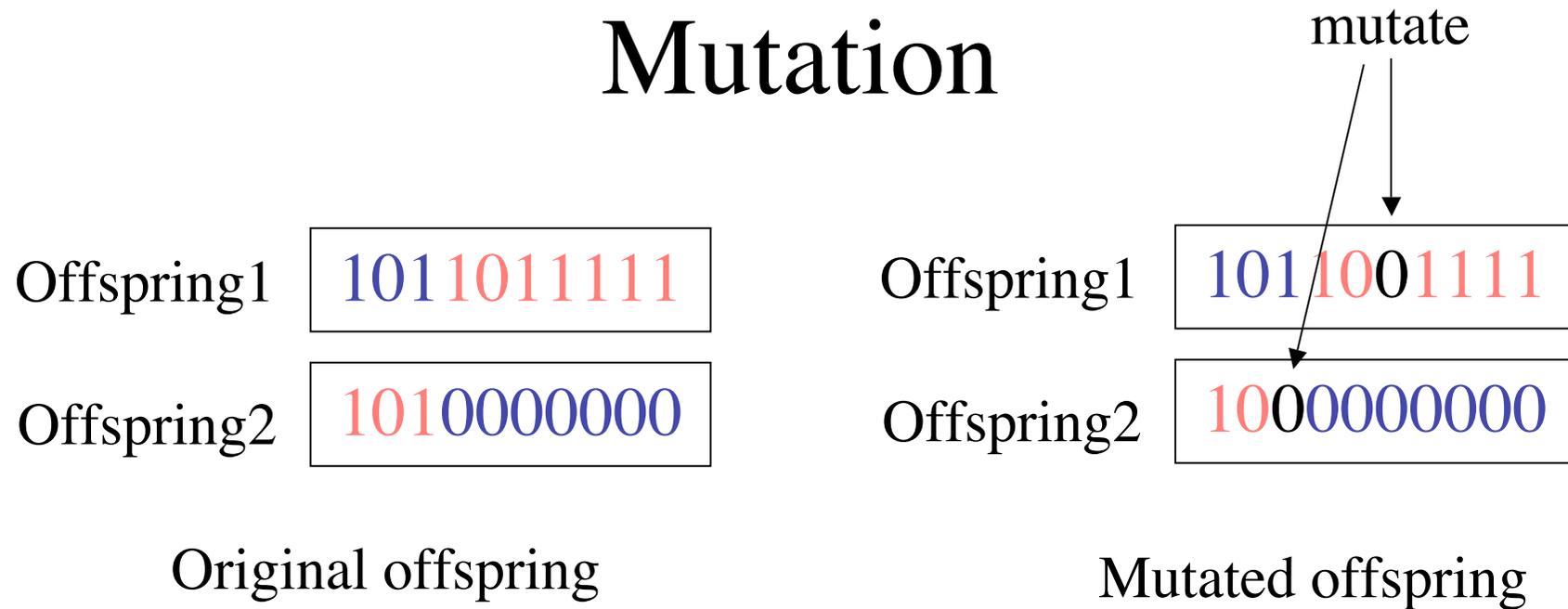


Crossover - Recombination



Crossover
single point -
random

Mutation



With some small probability (the *mutation rate*) flip each bit in the offspring (typical values between 0.1 and 0.001)

Back to the (GA) Algorithm

Generate a *population* of random chromosomes

Repeat (each generation)

 Calculate fitness of each chromosome

 Repeat

 Use roulette selection to select pairs of parents

 Generate offspring with crossover and mutation

 Until a new population has been produced

Until best solution is good enough

Many Variants of GA

- Different kinds of selection (not roulette)
 - Tournament
 - Elitism, etc.
- Different recombination
 - Multi-point crossover
 - 3 way crossover etc.
- Different kinds of encoding other than bitstring
 - Integer values
 - Ordered set of symbols
- Different kinds of mutation

Fitness functions

- Most GA's use explicit and static fitness function (as in our "oil" example)
- Some GA's (such as in Artificial Life or Evolutionary Robotics) use dynamic and implicit fitness functions - like "*how many obstacles did I avoid*"
- In these latter examples other chromosomes (robots) effect the fitness function

Question

- Going back to the OIL example
- Suppose we wanted to decide where to drill on a 2-dimensional area - like a whole desert
- How might we encode the chromosomes?